CS101C Type Theory and Formal Methods

Lecture 4

April 9, 2003



CS101C: Type Theory and Formal Methods

MetaPRL

MetaPRL is the latest in the PRL family of systems (λ -PRL, Micro-PRL, NuPRL, MetaPRL) developed over the last 25 years. MetaPRL (called NuPRL-Light at first) project was started by Jason Hickey in 1995. I joined the MetaPRL project in 1998.

MetaPRL contributors include:

- Caltech: Jason Hickey, Aleksey Nogin, Xin Yu, Brian Aydemir, Adam Granicz
- Cornell: Robert Constable, Alexei Kopylov, Lori Lorigo, Richard Eaton, Christoph Kreitz, Eli Barzilay
- CUNY: Sergei Artemov, Yegor Bryuhov
- Moscow State University: Vladimir Krupski
- Other: Stephan Schmitt, Carl Witty





General Theorem Prover Structure

From a very high-level point of view, a modern interactive prover can be divided into three parts:

- The core of the system its logical engine (or refiner [Bates 1979]) is in charge of handling primitive proof steps.
- Meta-theory and basic tactics provide a "support layer"; and
- Axiomatizations of *logical theories*, each potentially equipped with custom proof search, display and other mechanisms.





MetaPRL Structure

In MetaPRL refiner:

- Term module implements basic logical language.
- Rewriter module provides a mechanism for complex syntactical transformations.
- Proof accounting module keeps track of what have been proven.





MetaPRL Structure

In MetaPRL logical theories

Syntax definitions specify the language.

Inference rules define the primitive inferences. Example (axiom):

$\Gamma; A \vdash A$

- **Rewrites** define computational and definitional equivalences. Example $(\beta$ -reduction): $(\lambda x. b[x]) a \longleftrightarrow b[a]$
- Theorems provide proofs for derived inference rules and axioms.



Tactics provide theory-specific proof search automation.



Refiner

Tactics

In general, a *tactic* is a program that selects a proof steps for *logical engine* to perform.

- Tactics do not have to be correct
- Tactics are heuristics
- Tactics can potentially fail, make no progress, build a partial proof, or build a complete proof
- A simplest tactic is a single inference rule
- In MetaPRL, tactics are written in OCaml language, using a set of basic combinators (called *tacticals*).



Basic Tacticals

- I tryT tac tries applying tac (make no progress if tac fails).
- tac_1 then $T tac_2$ applies tac_1 , then on *all* subgoals it applies tac_2 . Fails is either tac fails.
- tac_1 orthenT tac_2 tries tac_1 , then (whether that works or not) on *all* subgoals it applies tac_2 .
- tac_1 orelseT tac_2 applies tac_1 , and if that fails, then applies tac_2 .
- onSomeHypT (OCaml type: (int -> tactic) ->
 tactic) applies its argument on each hypothesis number
 (from 1 to number of hypotheses) until first success.



Homework 2

Homework 2 will be posted tonight Due: Wednesday, Apr 16, at 2PM Task: Write several proofs in MetaPRL

